

Unit 5 Day 7L: Inequalities in One Triangle

AGENDA:

- Check & Review 5-6 Midsegment Homework
- Notes & Guided Practice

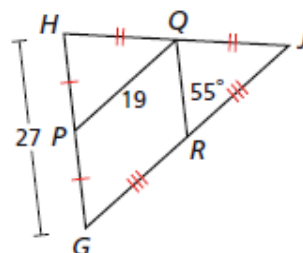
Homework - Day 8

- pg 336-37: #18,19,20, 21, 26, 32, 33, 34
- Continue to work on Constructions Project and lesson summaries both due test day

Day 6 HW Answers: p. 324-25: #11-16,18-20, 24,26

Find each measure.

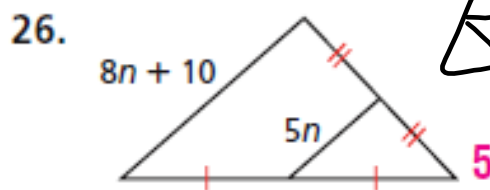
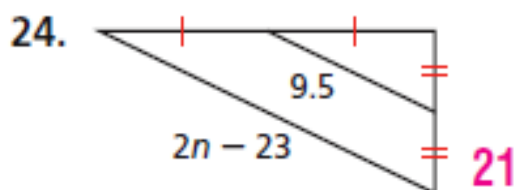
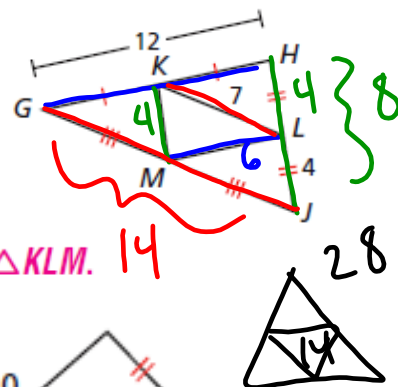
- |  |   |
|--|---|
| 11. $GJ$ <b>38</b>                             | 12. $RQ$ <b>13.5</b>                            |
| 13. $RJ$ <b>19</b>                             | 14. $m\angle PQR$ <b><math>55^\circ</math></b>  |
| 15. $m\angle HGJ$ <b><math>55^\circ</math></b> | 16. $m\angle GPQ$ <b><math>125^\circ</math></b> |



$\triangle KLM$  is the midsegment triangle of  $\triangle GHJ$ .

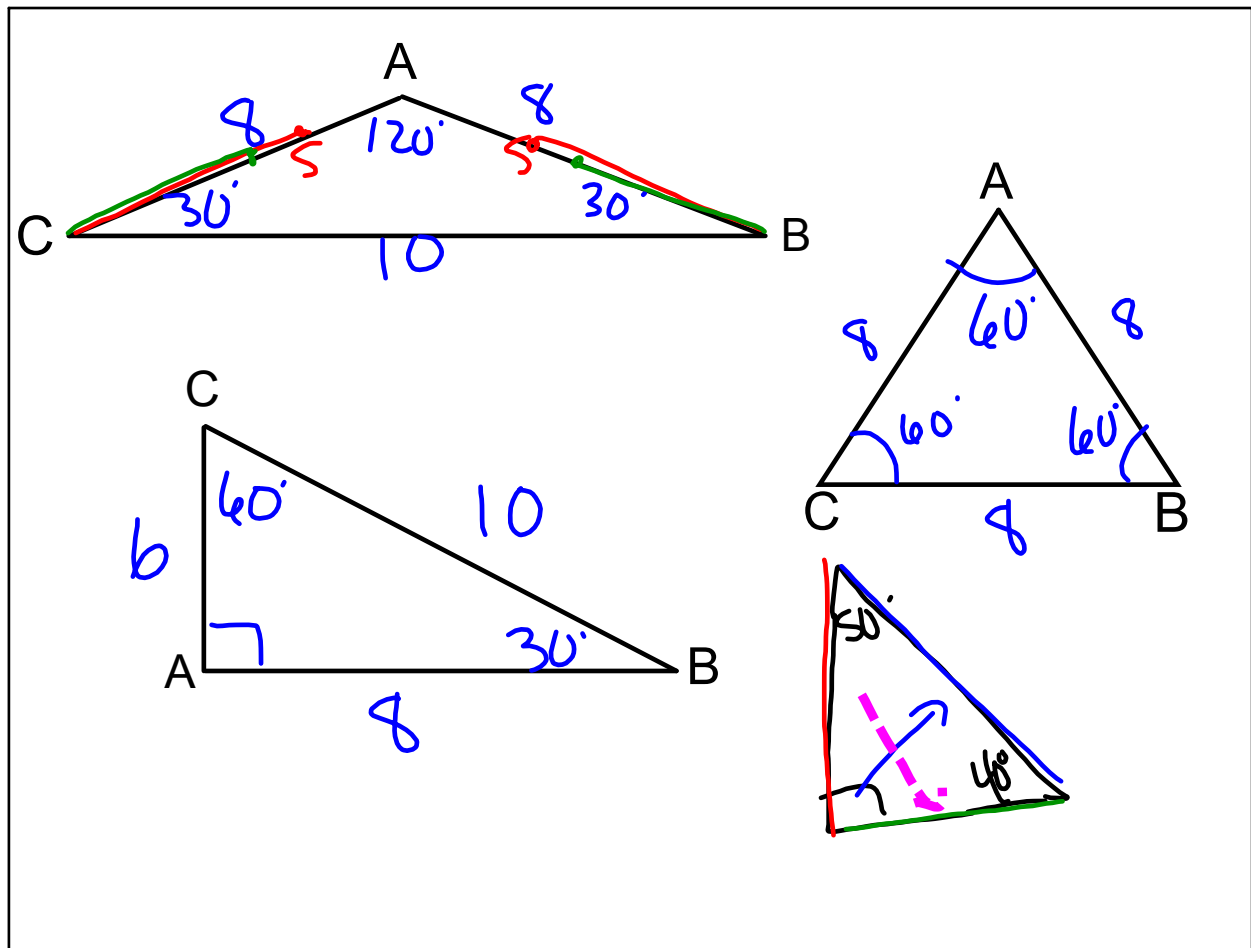
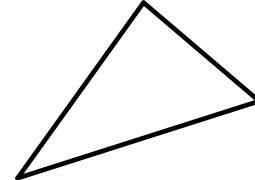
18. What is the perimeter of  $\triangle GHJ$ ? **34**
19. What is the perimeter of  $\triangle KLM$ ? **17**
20. What is the relationship between the perimeter of  $\triangle GHJ$  and the perimeter of  $\triangle KLM$ ?

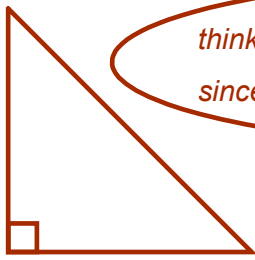
The perimeter of  $\triangle GHJ$  is twice the perimeter of  $\triangle KLM$ .



- Between you and your desk pair, draw the following using your UAM and a ruler:
  - > an isosceles obtuse triangle labeled ABC with the obtuse angle labeled A.
  - > an equiangular triangle labeled ABC.
  - > a scalene right triangle labeled ABC with the right angle labeled A.
- Using your triangles with your desk pair, measure and record the lengths of the sides of the triangle.

- What do you notice about the sides and angles?
- What do you notice about any combinations of sides?



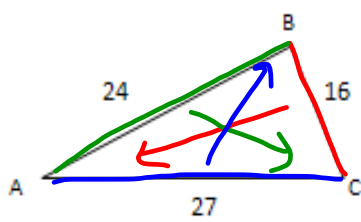


think right triangle, hypotenuse is ALWAYS the longest side, since it is across from the largest angle.

**Theorems** Angle-Side Relationships in Triangles

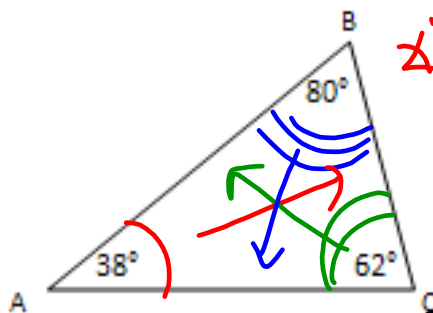
THEOREM	HYPOTHESIS	CONCLUSION
<p><b>5-5-1</b> If two sides of a triangle are not congruent, then the larger angle is opposite the longer side. (In <math>\triangle</math>, larger <math>\angle</math> is opp. longer side.)</p>	<p><math>AB &gt; BC</math></p>	<p><math>m\angle C &gt; m\angle A</math></p>
<p><b>5-5-2</b> If two angles of a triangle are not congruent, then the longer side is opposite the larger angle. (In <math>\triangle</math>, longer side is opp. larger <math>\angle</math>.)</p>	<p><math>m\angle Z &gt; m\angle Y</math></p>	<p><math>XY &gt; XZ</math></p>

1) List the Angles in Order from Smallest to Largest:



SIDES SHORTEST  $\rightarrow$  LONGEST  
 16 24 27  
 BC AB AC  
 $\angle$ 'S SMALLEST  $\rightarrow$  LARGEST  
 $\angle$  A  $\angle$  C  $\angle$  B

2) List the Sides in Order from Smallest to Largest:



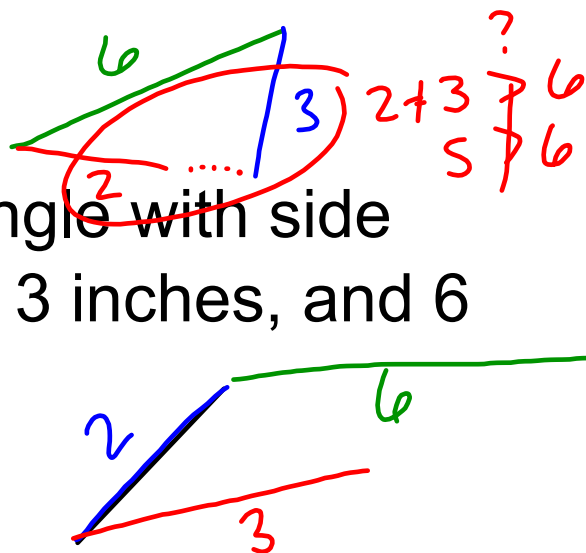
$\angle$ 'S SMALLEST  $\rightarrow$  LARGEST  
 38° 62° 80°  
 $\angle$  A  $\angle$  C  $\angle$  B  
 SIDES SHORTEST  $\rightarrow$  LARGEST  
 $\overline{BC}$   $\overline{AB}$   $\overline{AC}$

Oops - out of order;  
we'll come back to  
Regents Question #3

Try this:

Build a scalene triangle with side lengths of 2 inches, 3 inches, and 6 inches.

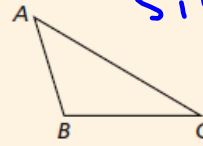
What happened?



**Theorem 5-5-3 Triangle Inequality Theorem**

The sum of any two side lengths of a triangle is greater than the third side length. *alone*

$$\begin{aligned} AB + BC &> AC \\ BC + AC &> AB \\ AC + AB &> BC \end{aligned}$$



*sum 2 sides > 3rd alone*

Sum of two smaller sides  
must be **greater than** 3rd side.  
 $\therefore$  Side 1 + Side 2 > Side 3

**Examples of determining if three sides can be the sides of a triangle:**

- 1) Can 5, 7, 12 be the sides of a triangle?      2) Can 2, 6, 7 be the sides of a triangle?

$$\begin{aligned} 5 + 7 &? 12 \\ 12 &\not> 12 \end{aligned}$$

**FALSE ONE COUNTEREX**

*NO, THE SUM OF 2 SIDES IS NOT ALWAYS GREATER THAN THE 3RD SIDE ALONE*

**TRUE - ALL 3 CASES MUST WORK**

$$\begin{aligned} 2 + 6 &? 7 & 2 + 7 &? 6 & 7 + 6 &? 2 \\ 8 &> 7 & 9 &> 6 & 13 &> 2 \\ \checkmark & & \checkmark & & \checkmark & \end{aligned}$$

**YES**  
**B/C THE SUM OF 2 SIDES IS ALWAYS > 3RD ALONE.**

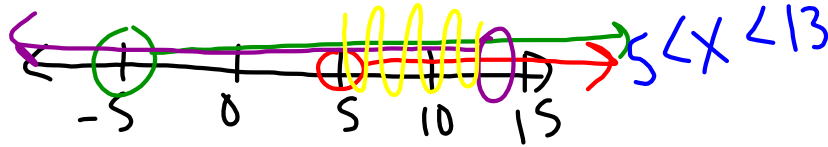
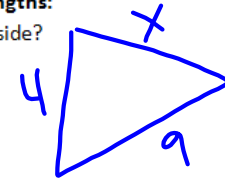
All three cases must be true or find one counterexample for false. Hint: try adding the two **smaller** sides.

Examples of finding the range of the length of the third side of triangle given two side lengths:

3) If two sides of a triangle are 4 and 9, what is the range of possible lengths of the third side?

To find min and max  
Min > side 1 - side 2  
Max < side 1 + side 2  
min < 3rd side < max

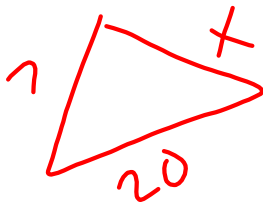
$$\begin{aligned}
 x+4 &> 9 & x+9 &> 4 & 4+9 &> x \\
 \underline{x > 5} & & \underline{x > -5} & & \underline{13 > x} & 
 \end{aligned}$$



What did you discover about the range of the sides of a triangle? Discover a shortcut:

$$9 - 4 < x < 9 + 4 \quad | \text{DIFF} | < x < \text{SUM}$$

4) If 2 sides of a triangle are 7 and 20, what is the range of values for the 3<sup>rd</sup> side?

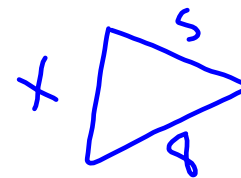


$$\begin{aligned}
 | \text{DIFF} | &< x < \text{SUM} \\
 20 - 7 &< x < 20 + 7 \\
 \boxed{13 < x < 27}
 \end{aligned}$$

5) (Regents Question) How many integer values of  $x$  are there so that  $x$ , 5, and 8 could be the lengths of the sides of a triangle?

- 1) 6
- 2) 9
- 3) 3
- 4) 13

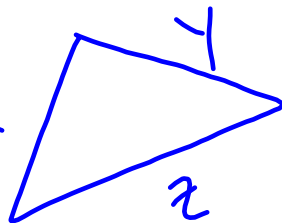
$$\begin{aligned}
 \text{DIFF} &< x < \text{SUM} \\
 8 - 5 &< x < 8 + 5 \\
 3 &< x < 13
 \end{aligned}$$



4, 5, 6, 7, 8, 9, 10, 11, 12

3) (Regents Question) Phil is cutting a triangular piece of tile. If the triangle is scalene, which set of numbers could represent the lengths of the sides?

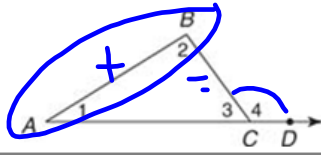
- ~~1) {2, 4, 7}~~  $2+4 \not> 7$
  - 2) {4, 5, 6}
  - ~~3) {3, 5, 8}~~  $3+5 \not> 8$
  - ~~4) {5, 5, 8}~~  $5+5 \not> 8$
- NOT SCALENE



SUM 2 SIDES > 3<sup>RD</sup>?

If time allows...

**Exterior Angle Inequality Theorem:** The measure of an exterior angle of a triangle is greater than the measure of each of its remote interior angles.



$$m\angle 4 > m\angle 1 \quad \text{and} \quad m\angle 4 > m\angle 2$$

$$m\angle 1 + m\angle 2 = m\angle 4 \quad \text{EXT}\angle$$

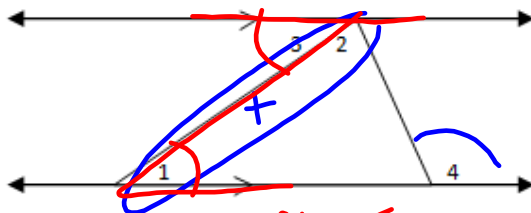
$$30 + 50 = 80 \quad \text{Thm}$$

$$20 + 70 = 90$$

$$20 + 100 = 120$$

**EXAMPLE:**

Explain why  $m\angle 4 > m\angle 3$ .



$\parallel \rightarrow \cong \text{ALT INT}$

$$m\angle 4 > m\angle 1$$

$$m\angle 4 > m\angle 3 \quad \text{SUBST.}$$



COOR  
PROOFS

RIGID  
MOTIONS

TRIANGLE  
PROOFS USING  
CRITERIA +  
CPCTC