

AGENDA - Unit 10-4

*Spheres and Quiz*

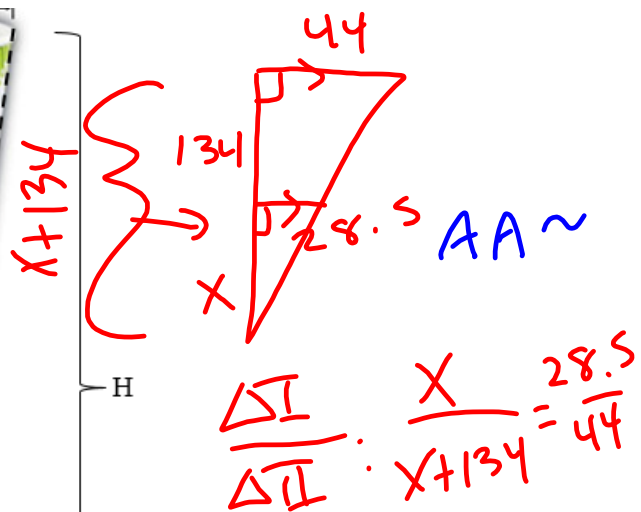
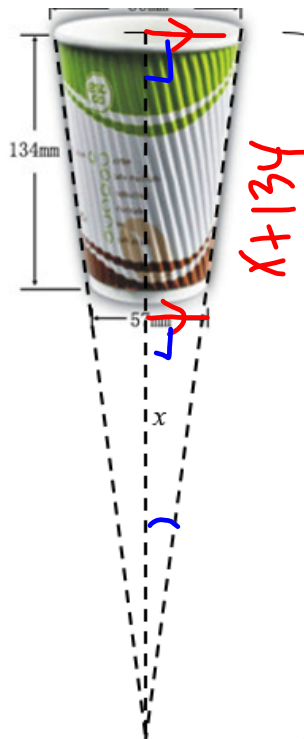
- Go over HW 10.3
- Quiz
- Notes 10.4
- HW - 10.4



5. A Dixie cup is like a truncated cone with bases of 88 mm and 57 mm and a height of 134 mm.

A. Determine the height  $H$  of the full cone to the nearest tenth of a mm.

B. Explain how you arrived at your answer.



6) Backsolving: If the volume of a right cone is  $320\pi \text{ ft}^3$  with an altitude of 5 ft, what is the radius of the cone?

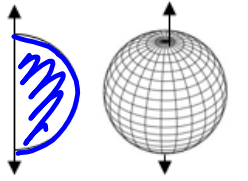
7) A pyramid has a volume of  $24 \text{ ft}^3$  with a height of 6 ft. What is the area of the base?

8) Suppose you fill a conical paper cup with a height of 6" with water. If all the water is then poured into a cylindrical plastic cup with the same radius and same height as the conical paper cup, to what height will the water reach in the cylindrical plastic cup?

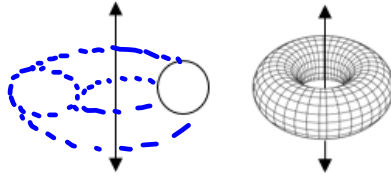
Geometry + LAB Name \_\_\_\_\_ Section \_\_\_\_\_ Date \_\_\_\_\_

10-4R & 10-7L Notes: Spheres

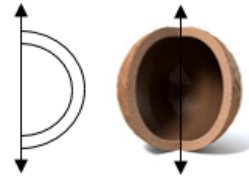
Creation of Other Solids by Rotation:



SPHERE



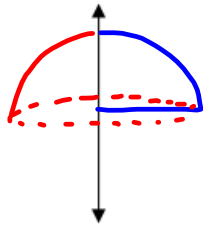
TORUS



HOLLOW  
CORE SPHERE

What 2-D shape could be rotated to produce just the Northern Hemisphere? What role does the Equator play?

Look at other slices as well:



GREAT  
CIRCLE



SLICES  
ARE ○'S

**Definition of a Sphere:**

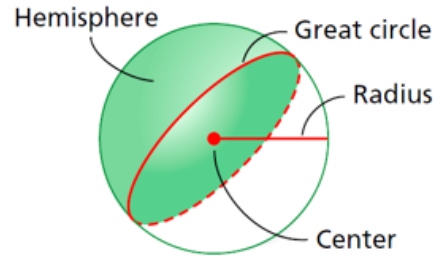
The set of all points equidistant from a central point.  
 A solid sphere therefore is the set of all points less than or equal to the radius.

**Surface Area Formula**

$$SA = 4\pi r^2$$

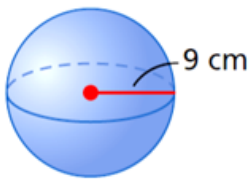
**Volume Formula**

$$V = \frac{4}{3}\pi r^3$$



Practice:

- 1) Find the volume of the sphere in terms of  $\pi$ :



C  
A  
 $r = 9 \text{ cm}$   
D

$$\begin{aligned} V &= \frac{4}{3}\pi r^3 = \frac{4}{3}\pi (9)^3 \\ &= \frac{4}{3}\pi (729) \\ &= \boxed{972\pi \text{ cm}^3} \end{aligned}$$

2) Find the radius of the sphere with a volume of  $125\pi \text{ in}^3$ .

$$V = \frac{4}{3}\pi r^3$$

$$\left(\frac{3}{4}\right) 125\pi \text{ in}^3 = \frac{4}{3}\pi r^3 \left(\frac{3}{4}\right)$$

$$\frac{3}{4}(125) = r^3$$

$$\sqrt[3]{\frac{375}{4}} = \sqrt[3]{r^3}$$

MATH : 4  $\Rightarrow$   $\sqrt[3]{375/4}$

4.5428

$4.5 \text{ IN} = r$

3) Find the volume of the sphere with a great circle that has an area of  $49\pi \text{ in}^2$ .



C

$$A = 49\pi \text{ IN}^2 = \pi r^2$$

R = 7 IN

$$49\pi = \pi r^2$$

$$49 = r^2$$

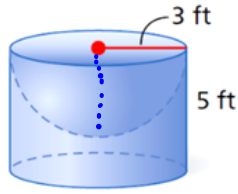
$$\oplus \sqrt{49} = r$$

$$7 = r$$

$$V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi(7)^3$$

$$= \frac{1372\pi}{3} \text{ IN}^3$$

4) Find the volume of the composite solid to the nearest tenth of a cubic foot:



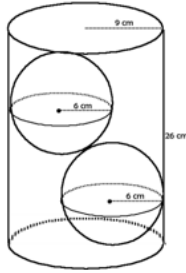
$$\begin{array}{l} C \\ A = \pi r^2 = \pi 3^2 \\ \boxed{R=3} \\ D \end{array} = 9\pi \text{ FT}^2$$

$$\begin{array}{l} V_{\text{CYL}} = BH \\ = (9\pi) 5 \\ = 45\pi \end{array} \quad \left| \quad \begin{array}{l} V_{\text{SPH}} = \frac{1}{2} V_{\text{SPH}} \\ = \frac{1}{2} \left( \frac{4}{3} \pi r^3 \right) \\ = \frac{1}{2} \left( \frac{4}{3} \pi (3^3) \right) \\ = 36\pi \end{array} \right.$$

$$\begin{aligned} V_{\text{COMPOSITE}} &= 45\pi - \frac{1}{2}(36\pi) \\ &= 45\pi - 18\pi \\ &= 27\pi \\ &= 84.8230 \\ &\boxed{\approx 84.8 \text{ FT}^3} \end{aligned}$$

$$100 - 3\pi \neq 97\pi$$

5) Find the fraction of the can's volume taken up by the two spheres:



$$\frac{2V_{SPH}}{V_{CAN}} = \text{FRACTION}$$

$$\frac{2\left(\frac{4}{3}\pi r_s^3\right)}{\pi r_c^2 H} = \frac{2\left(\frac{4}{3}\pi 6^3\right)}{\pi 9^2(26)}$$

$$\frac{\frac{8}{3}\pi 216}{2106\pi} = \frac{576\pi}{2106\pi}$$

0.2735

MATH 1:  $\blacktriangleright$  FRAC

$$\boxed{\frac{32}{117}}$$

$$r \rightarrow 3r$$

6) The radius of a sphere is tripled. Will this produce a similar sphere? Describe the effect on the

a. Volume

$$\frac{\frac{4}{3}\pi r^3}{1r^3} \quad \frac{\frac{4}{3}\pi (3r)^3}{27r^3}$$

b. Surface Area

$k^2 = 9 \times$   
THE  
AREA

27 TIMES AS BIG

$$k = 3$$

$$k^3 = 27$$