

## Review Day

Verify that:  $(\csc x - \cot x)^2 = \frac{1 - \cos x}{1 + \cos x}$

$$(\csc x - \cot x)(\csc x - \cot x)$$

$$\csc^2 x - \csc x \cot x - \csc x \cot x + \cot^2 x$$

$$\csc^2 x - 2 \csc x \cot x + \cot^2 x$$

$$\frac{1}{\sin^2 x} - 2 \frac{1}{\sin x} \cdot \frac{\cos x}{\sin x} + \frac{\cos^2 x}{\sin^2 x}$$

$$\frac{1}{\sin^2 x} - \frac{2 \cos x}{\sin^2 x} + \frac{\cos^2 x}{\sin^2 x}$$

$$\frac{1 - 2 \cos x + \cos^2 x}{\sin^2 x} \rightarrow \frac{\overset{-1}{\cancel{\cos x - 1}}(\cos x - 1)}{\sin^2 x - 2 \cos x + 1}$$

$$\frac{1 - \cos^2 x}{(1 - \cos x)(1 + \cos x)}$$

$$\frac{-\cos x + 1}{1 + \cos x}$$

$$\frac{\overset{-1}{(x-1)}(x+1)}{1-x^2} = \frac{-x+1}{x+1}$$

$$\frac{(1-x)(1+x)}{(1-x)(1+x)}$$

$$\begin{aligned}
 \textcircled{1} \quad & \frac{\sec \theta}{\cos \theta} - \frac{\tan \theta}{\cot \theta} = 1 \\
 & \frac{1 \cdot \cancel{\cos \theta}}{\cancel{\cos \theta} \cdot \cos \theta} - \frac{\cancel{\sin \theta} \cdot \cancel{\cos \theta} \sin \theta}{\cancel{\cos \theta} \cdot \cancel{\cos \theta} \sin \theta} \\
 & \frac{1}{\cos^2 \theta} - \frac{\sin^2 \theta}{\cos^2 \theta} \\
 & \frac{1 - \sin^2 \theta}{\cos^2 \theta} \\
 & \frac{\cos^2 \theta}{\cos^2 \theta} \\
 & 1 = 1
 \end{aligned}$$

• Q.F.  
 • Ident.  
 Notes

$$\textcircled{2} \frac{(\cos^2\theta) \cdot 1}{(\cos^2\theta) \sin^2\theta} + \frac{1 \cdot \sin^2\theta}{\cos^2\theta (\sin^2\theta)} = (\sec^2\theta)(\csc^2\theta)$$

$$\frac{\cos^2\theta + \sin^2\theta}{\cos^2\theta \sin^2\theta}$$

$$\frac{1}{\cos^2\theta \sin^2\theta}$$

$$\frac{1}{\cos^2\theta} \cdot \frac{1}{\sin^2\theta}$$

$$\sec^2\theta \cdot \csc^2\theta$$

$$\frac{1}{4.5} = \frac{1}{4} \cdot \frac{1}{5}$$